

# Semantic Theory

## week 8 – DRT: Syntax and Interpretation

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# Mass nouns again (exercise sheet 5, ex. 2)

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To interpret mass nouns, we use the model  $M = \langle \langle U, \leq_i \rangle, \langle M, \leq_m \rangle, V \rangle$ , where:

- $U \cap M = \emptyset$
- $\langle U, \leq_i \rangle$  is an atomic join semi-lattice
- $\langle M, \leq_m \rangle$  is a non-atomic and dense join semi-lattice
- $V$  is a value assignment function
- Variables referring to matters:  $\mathbf{x}, \mathbf{y}, \mathbf{z}, \dots$
- A material fusion operation  $\oplus_m$  and a material part relation  $\triangleleft_m$  (to be distinguished from  $\oplus_i$  and  $\triangleleft_i$ , respectively)
- $\llbracket m(\alpha) \rrbracket^{M, g} = h(\llbracket \alpha \rrbracket^{M, g})$ , where  $\alpha \in WE_e$  is a well-formed expression denoting an individual entity

# DRS Syntax

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A discourse representation structure (DRS)  $K$  is a pair  $\langle U_K, C_K \rangle$ , where:

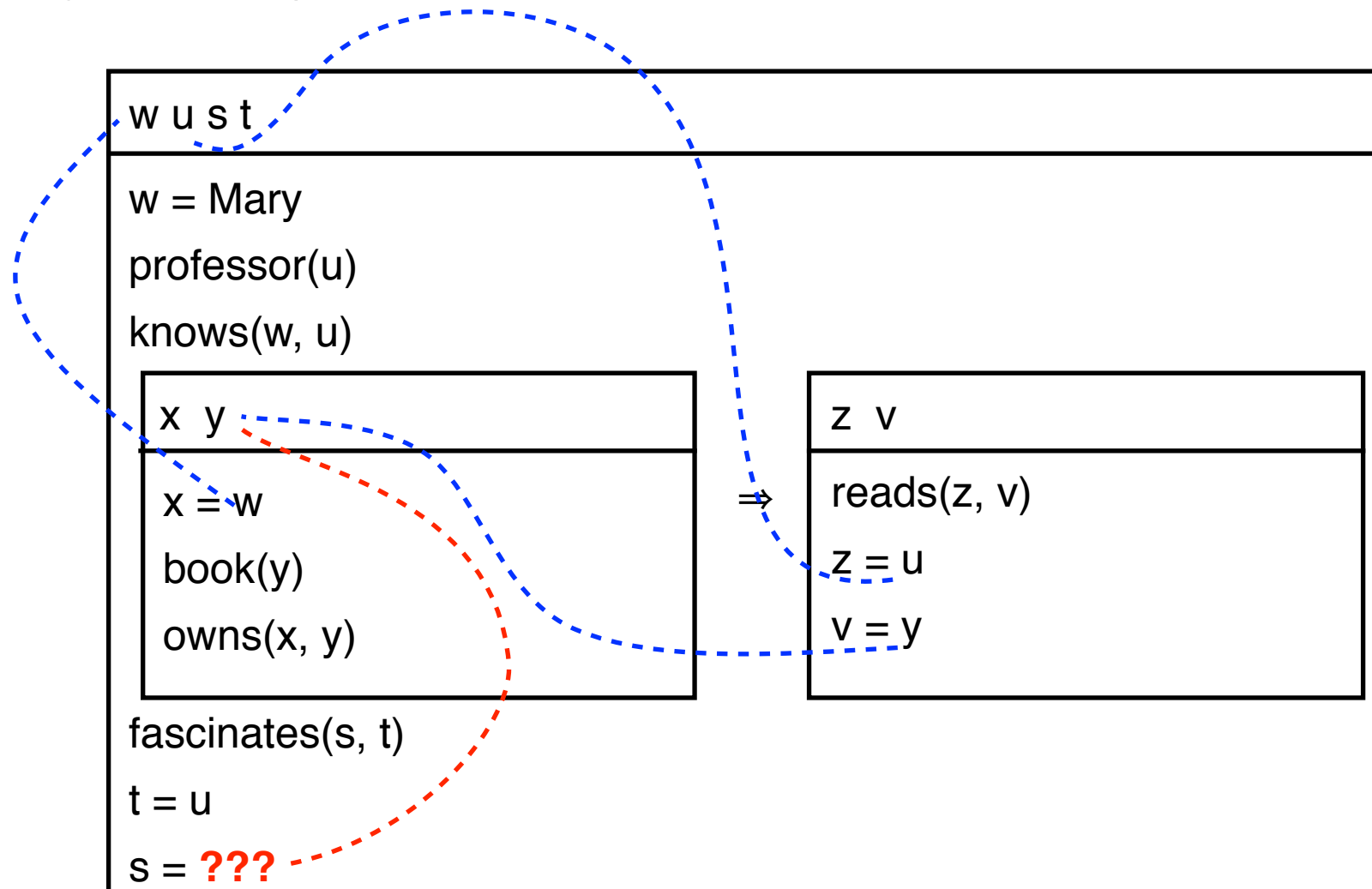
- $U_K \subseteq U_D$  and  $U_D$  is a set of discourse referents, and
- $C_K$  is a set of well-formed DRS conditions

## Well-formed DRS conditions:

- $R(u_1, \dots, u_n)$       *where:*  $R$  is an  $n$ -place relation,  $u_i \in U_D$
- $u = v$        $u, v \in U_D$
- $u = a$        $u \in U_D$ ,  $a$  is a constant
- $\neg K_1$        $K_1$  is a DRS
- $K_1 \Rightarrow K_2$        $K_1$  and  $K_2$  are DRSs
- $K_1 \vee K_2$        $K_1$  and  $K_2$  are DRSs

# Anaphora and accessibility

*Mary knows a professor. If she owns a book, he reads it. ?It fascinates him.*



# Non-accessible discourse referents

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## Cases of non-accessibility:

- (1) *If a professor owns a book, he reads it. It has 300 pages.*
- (2) *It is not the case that a professor owns a book. He reads it.*
- (3) *Every professor owns a book. He reads it.*
- (4) *If every professor owns a book, he reads it.*
- (5) *Peter owns a book, or Mary reads it.*
- (6) *Peter reads a book, or Mary reads a newspaper article. It is interesting.*

# Accessible discourse referents

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The following discourse referents are accessible for a condition:

- DRs in the same local DRS
- DRs in a superordinate DRS
- DRs in the universe of an antecedent DRS, if the condition occurs in the consequent DRS.

We need a formal notion of DRS subordination

# Subordination

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A DRS  $K_1$  is an immediate sub-DRS of a DRS  $K = \langle U_K, C_K \rangle$  iff  $C_K$  contains a condition of the form

- $\neg K_1, K_1 \Rightarrow K_2, K_2 \Rightarrow K_1, K_1 \vee K_2$  or  $K_2 \vee K_1$ .

$K_1$  is a sub-DRS of  $K$  (notation:  $K_1 \leq K$ ) iff

- $K_1 = K$ , or
- $K_1$  is an immediate sub-DRS of  $K$ , or
- there is a DRS  $K_2$  such that  $K_2 \leq K_1$  and  $K_1$  is an immediate sub-DRS of  $K$  (i.e. reflexive, transitive closure)

$K_1$  is a proper sub-DRS of  $K$  iff  $K_1 \leq K$  and  $K_1 \neq K$ .

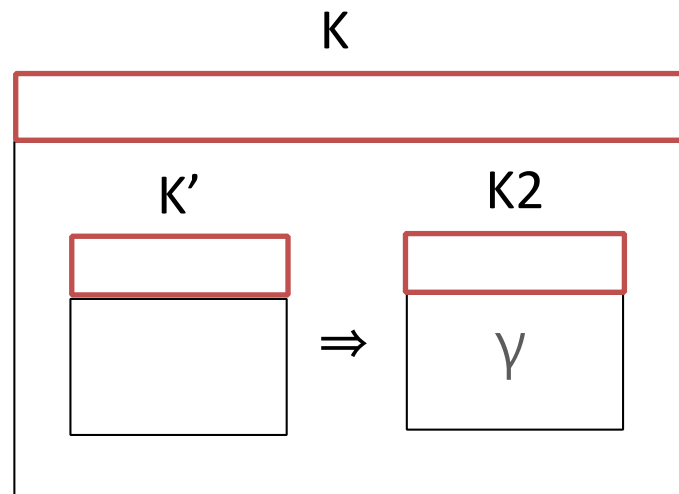
# Accessibility

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Let  $K, K_1, K_2$  be DRSs such that  $K_1, K_2 \leq K$ ,  $x \in U_{K_1}$ ,  $\gamma \in C_{K_2}$

$x$  is accessible from  $\gamma$  in  $K$  iff

- $K_2 \leq K_1$  or
- there are  $K_3, K_4 \leq K$  such that  $K_1 \Rightarrow K_3 \in C_{K_4}$  and  $K_2 \leq K_3$





# Free and bound variables in DRT

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A DRS variable  $x$ , introduced in DRS  $K_1$ , is bound in global DRS  $K$  iff there exists a DRS  $K_j \leq K$ , such that:

(i)  $K_i \leq K_j$ ;

(ii)  $x \in U(K_j)$ .

**Properness:** A DRS is *proper* iff it does not contain any free variables

**Purity:** A DRS is *pure* iff it does not contain any *otiose declarations* of variables

$x \in U(K_1)$  and  $x \in U(K_2)$  and  $K_1 \leq K_2$



# Playing in the sandbox

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**PDRT-SANDBOX** is a Haskell library that implements Discourse Representation Theory (and its extension Projective Discourse Representation Theory)

<http://hbrouwer.github.io/pdrt-sandbox/>




- Define your own DRSs, using the internal syntax or the set-theoretic notation
- Show the DRSs in different output formats (boxes, linear boxes, set-theoretic, internal syntax)
- Composition of DRSs (more on that next week)
- Translate DRSs to FOL formulas
- ... and more!

# DRS Syntax in PDRT-SANDBOX

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DRS:            DRS [ ... ] [ ... ]    referents    conditions



Referents:     DRSRef "x", DRSRef "Mary"

Conditions:

Relation:       Rel (DRSRel "man") [DRSRef "x"]

Identity:       Rel (DRSRel "=") [DRSRef "x", DRSRef "y"]

Negation:       Neg (DRS [ ... ] [ ... ])

Implication:    Imp (DRS [ ... ] [ ... ]) (DRS [ ... ] [ ... ])

Disjunction:    Or (DRS [ ... ] [ ... ]) (DRS [ ... ] [ ... ])

Properties:      isPure(DRS [ ... ] [ ... ]), isProper(DRS [ ... ] [ ... ])

# This week's take-home assignment:

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- Download and install PDRT-SANDBOX

<http://hbrouwer.github.io/pdrt-sandbox/>

- Get familiar with the software by trying out the DRS tutorial

<https://github.com/hbrouwer/pdrt-sandbox/blob/master/tutorials/DRSTutorial.hs>

(you can skip the part about “Combining DRSs” for now)

- Playing in the sandbox: create your own DRSs, and see what else you can do with it.