

Semantic Theory: Discourse Semantics I

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M.Pinkal/ S. Thater



A simple context theory (Lewis 1970/72)



- Model contexts as vectors: sequences of semantically relevant context data with fixed arity.
- Model meanings as functions from contexts to denotations - more specifically, as functions from certain components of contexts to denotations.

Semantic Context Dependence



- Some natural-language expressions, like *I*, *you*, *here*, *this*, vary their meaning with context.

An Example



- Context $c = \langle a, b, l, t, r \rangle$

- <i>a</i> speaker	$[[I]]^{M,g,c} = \text{utt}(c) = a$
- <i>b</i> addressee	$[[you]]^{M,g,c} = \text{adr}(c) = b$
- <i>l</i> utterance location	$[[here]]^{M,g,c} = \text{loc}(c) = l$
- <i>t</i> utterance time	$[[now]]^{M,g,c} = \text{time}(c) = t$
- <i>r</i> referred object	$[[this]]^{M,g,c} = \text{ref}(c) = r$

Type-theoretic context semantics



- Model structure: $M = \langle U, C, V \rangle$
 - U model universe
 - C context set
 - V value assignment function that assigns non-logical constants functions from contexts to denotations of appropriate type.
- Interpretation:
 - $[[\alpha]]^{M,h,c} = V(\alpha)(c)$, if α non-logical constant,
 - $[[\alpha]]^{M,h,c} = h(\alpha)$, if α Variable,
 - $[[\alpha(\beta_1, \dots, \beta_n)]]^{M,h,c} = [[\alpha]]^{M,h,c}([[\beta_1]]^{M,h,c}, \dots, [[\beta_n]]^{M,h,c})$
 - etc.

Interpretation: An example



I am reading this book \Rightarrow $\text{read}'(\text{this-book})(I')$

$[[\text{read}'(\text{this-book})(I')]]^{M,h,c} =$

$[[\text{read}']]^{M,h,c}([[\text{this-book}]]^{M,h,c})([[I']]^{M,h,c}) =$

$V(\text{read}')(\text{ref}(c))(\text{utt}(c))$

Note: context-invariant expressions are interpreted as constant functions:

$V(\text{read}')(\text{c}) = V(\text{read}')(\text{c}') [= V(\text{read}')] \text{ for all } c, c' \in C$

A simple dichotomy of context-dependent expressions



- **Deictic expressions** depend on the physical utterance situation:
I, you, now, here
- **Anaphoric expressions** refer to linguistic context/previous discourse:
he, she, it, then

Context Dependence: The Real Story



- Context dependence in natural language is pervasive

Every student must be familiar with the basic properties of FOL

John always is late.

It is hot and sunny everywhere.

Bill has bought an expensive car.

Another one, please!

- The relation between context and meaning is much more complex than the simple theory suggests.

Definite NPs are context-dependent expressions



- Standard type-theoretic representation of definite article:

the $\Rightarrow \lambda F \lambda G \exists y (\forall x (F(x) \leftrightarrow x=y) \wedge G(y))$

the sun $\Rightarrow \lambda G \exists y (\forall x (sun'(x) \leftrightarrow x=y) \wedge G(y))$

the sun is shining \Rightarrow

$\exists y (\forall x (sun'(x) \leftrightarrow x=y) \wedge shine'(y))$

the student is working \Rightarrow

$\exists y (\forall x (student'(x) \leftrightarrow x=y) \wedge work'(y))$???

- Definite NPs pick an appropriate object from context.

How do definite NPs depend on context?



- Utterances typically contain several noun phrases referring to different objects:
The student is reading the book in the library
- Noun phrases may refer to different objects of the same type, in one utterance situation:

the book

the blue book

the blue book about discourse semantics

The interaction of definite and indefinite NPs



- In texts, there is a division of labor between indefinite and definite NPs:

A student is working. The student/ She is successful.

- Indefinite noun phrases establish the context for later reference, they introduce new reference objects.
- Definite noun phrases (pronouns or full NPs) refer to familiar objects which have been introduced into the text before, e.g. by indefinite NPs.

The interaction of definite and indefinite NPs



- Standard type-theoretic analysis of indefinite NP:

a $\Rightarrow \lambda P \lambda Q \exists x [P(x) \wedge Q(x)]$

a student $\Rightarrow \lambda Q \exists x [student'(x) \wedge Q(x)]$

A student is working $\Rightarrow \exists x [student'(x) \wedge work'(x)]$

she $\Rightarrow \lambda PP(x)$

She is successful $\Rightarrow successful'(x)$

A student is working. She is successful.

$\Rightarrow \exists x [student'(x) \wedge work'(x)] \wedge successful'(x)$

- The variable representing anaphoric pronoun is unbound.
- Standard type-theoretic interpretation is insufficient to model the dynamics of context-meaning interaction.

The interaction of definite and indefinite NPs



- Natural-language utterances and context may interact in a twofold way:
On the one side, context determines the utterance meaning, on the other side, the utterance changes the context.
- The „context change potential“ is part of the meaning of natural-language expressions.

Yet another complication



- Reference objects in discourse need not be real objects:
*Someone - whoever that may be - will eventually find out. **That person** will tell others, and everyone will be terribly upset.*
*If you have a pencil or a ballpoint pen, could you please pass **it** to me?*

Context dependence: Wrap up



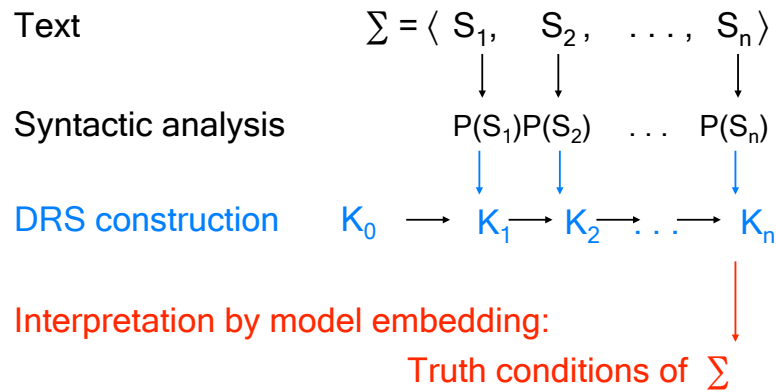
- The interpretation of most context-dependent expressions, e.g., **definite noun phrases**, is determined by context in a complex way.
- Some types of expressions, like **indefinite noun phrases**, introduce new context information, which is available at a later stage of discourse for anaphoric reference. Modelling this kind of **context change potential** is outside the reach of standard type-theoretic semantics, with or without context-semantic extension.
- The entities involved in contextual reference are not real objects, but a more abstract kind of entities.

Discourse Semantics



- The basic idea: Meaning as **Context Change Potential**
- Focus on anaphoric use of noun phrases (definite and indefinite, full NPs and pronouns).
- Meaning representation uses **discourse referents** in addition to formulas encoding truth conditions.
- "Division of labor" between definite and indefinite NPs:
 - Indefinite NPs introduce new discourse referents
 - Definite NPs refer to "old" or "familiar" discourse referents (which are already part of the meaning representation)
- Discourse Representation Theory: Hans Kamp (1981), Irene Heim (1980)
- **Reading: Hans Kamp/Uwe Reyle: From Discourse to Logic, Kluwer: Dordrecht 1993.**

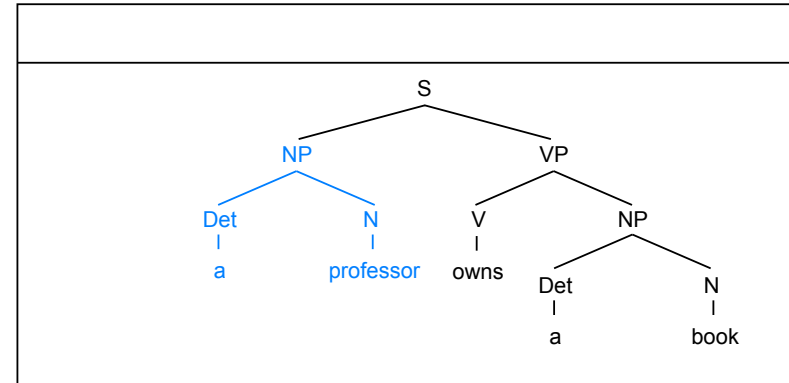
Discourse Representation Theory (DRT)



An example



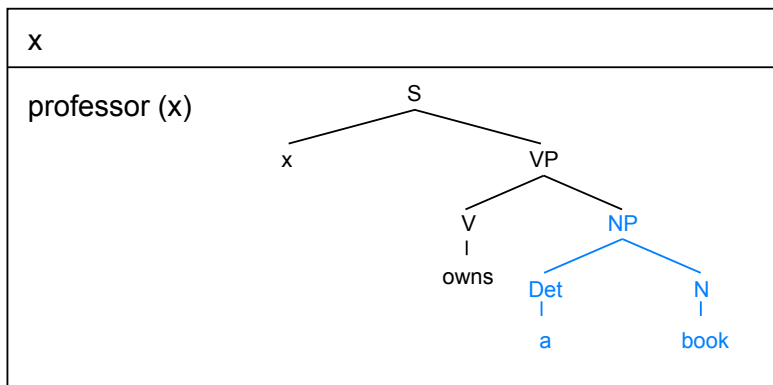
- *A professor owns a book. He reads it.*



An example



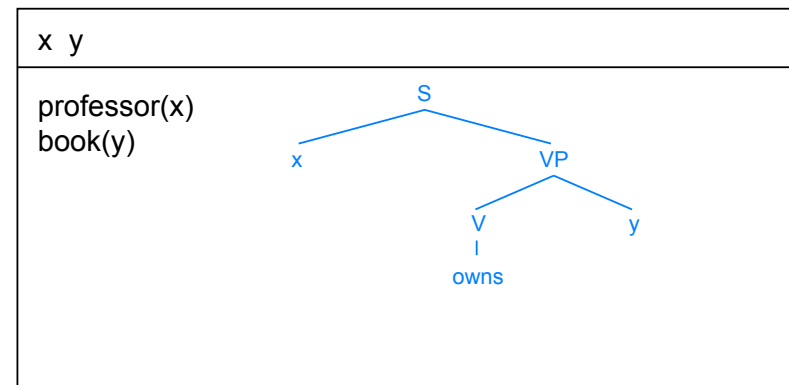
- *A professor owns a book. He reads it.*



An example



- *A professor owns a book. He reads it.*



An example



- *A professor owns a book. He reads it.*

x y
professor(x) book(y) own(x, y)

An example



- *A professor owns a book. He reads it.*

x y
professor(x) book(y) own(x, y) <pre>graph TD S --- NP1[NP] S --- VP NP1 --- he[he] VP --- V[V] VP --- NP2[NP] V --- reads[reads] NP2 --- it[it]</pre>

An example



- *A professor owns a book. He reads it.*

x y z
professor(x) book(y) own(x, y) z = x <pre>graph TD S --- z[z] S --- VP VP --- V[V] VP --- NP[NP] V --- reads[reads] NP --- it[it]</pre>

An example



- *A professor owns a book. He reads it.*

x y z u
professor(x) book(y) own(x, y) z = x u = y <pre>graph TD S --- z[z] S --- VP VP --- V[V] VP --- u[u] V --- reads[reads]</pre>

An example



- *A professor owns a book. He reads it.*

x	y	z	u
professor(x)			
book(y)			
own(x, y)			
$z = x$			
$u = y$			
read(z, u)			

DRS (Basic Version)



- A discourse representation structure (DRS) K is a pair $\langle U_K, C_K \rangle$, where
 - U_K is a set of **discourse referents**
 - C_K is a set of **conditions**
- (Fully reduced) conditions:
 - $R(u_1, \dots, u_n)$ R n-place relation, $u_i \in U_K$
 - $u = v$ $u, v \in U_K$
 - $u = a$ $u \in U_K, a$ is proper name
- **Reducible conditions**: Conditions of form α or $\alpha(x_1, \dots, x_n)$, where α is a context-free parse tree.

DRS (Basic Version)



- A discourse referent (DR) u is free in DRS $K = \langle U_K, C_K \rangle$, if u is free in one of K 's conditions, and $u \notin U_K$.
- A DRS K is closed in K iff no DR occurs free in K .
- A reducible (fully reduced) DRS is a DRS which contains (does not contain) reducible conditions.

DRS Construction Algorithm



- Input:
 - a text $\Sigma = \langle S_1, \dots, S_n \rangle$
 - a DRS $K_0 (= \langle \emptyset, \emptyset \rangle)$, by default
- Repeat for $i = 1, \dots, n$:
 - Add parse tree $P(S_i)$ to the conditions of K_{i-1} .
 - Apply DRS construction rules to reducible conditions of K_{i-1} , until no reduction steps are possible any more. The resulting DRS is K_i , the discourse representation of text $\langle S_1, \dots, S_i \rangle$.

DRS Construction Rule for Indefinite NP



- Triggering Configuration:
 - α is reducible condition in DRS K , containing $[_{S}[_{NP} \beta] [_{VP} \gamma]]$ or $[_{VP} [_{V} \gamma] [_{NP} \beta]]$ as a substructure.
 - β is $\varepsilon\delta$, ε indefinite article
- Action:
 - Add a new DR x to U_K .
 - Replace β in α by x .
 - Add $\delta(x)$ to C_K .

DRS Construction Rule for Personal Pronoun



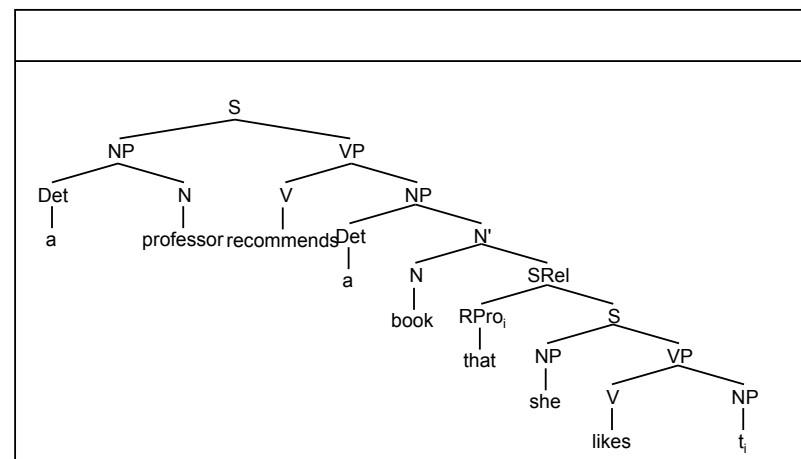
- Triggering Configuration:
 - α is reducible condition in DRS K ; α contains $[_{S}[_{NP} \beta] [_{VP} \gamma]]$ or $[_{VP} [_{V} \gamma] [_{NP} \beta]]$ as substructure.
 - β is a personal pronoun.
- Action:
 - Add a new DR x to U_K .
 - Replace β in α by x .
 - Select an appropriate DR $y \in U_K$, and add $x = y$ to C_K .

DRS Construction Rule for Proper Names

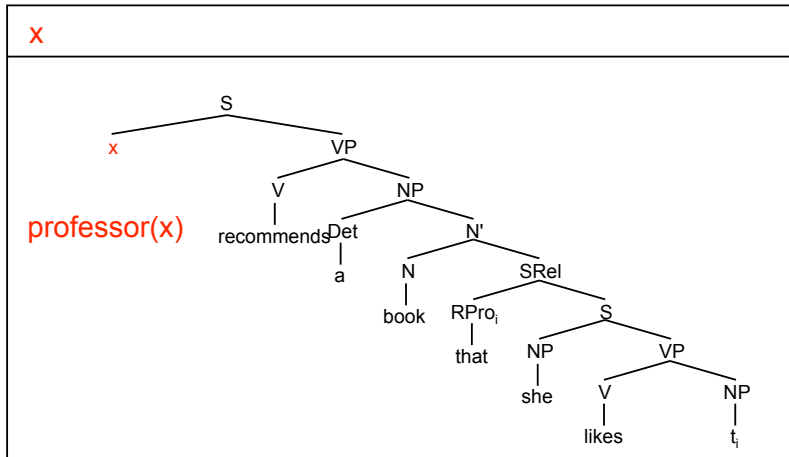


- Triggering Configuration:
 - α is reducible condition in DRS K ; α contains $[_{S}[_{NP} \beta] [_{VP} \gamma]]$ or $[_{VP} [_{V} \gamma] [_{NP} \beta]]$ as substructure.
 - β is a proper name.
- Action:
 - Add a new DR x to U_K .
 - Replace β in α by x .
 - Add $x = \beta$ to C_K .

A more complex example



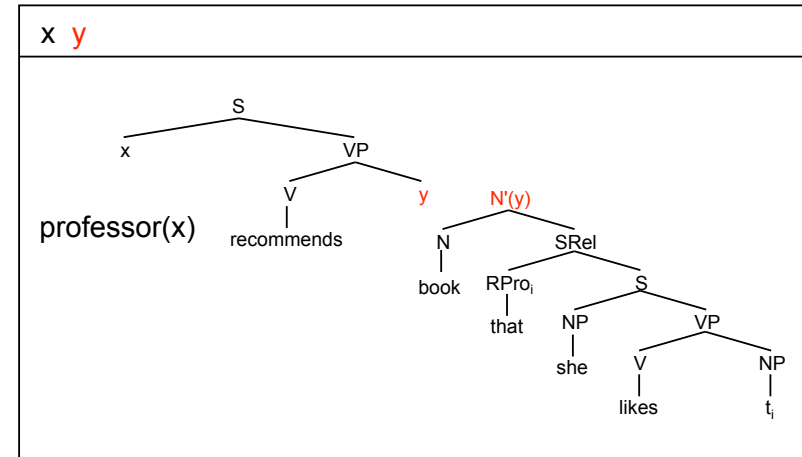
Indefinite NP rule



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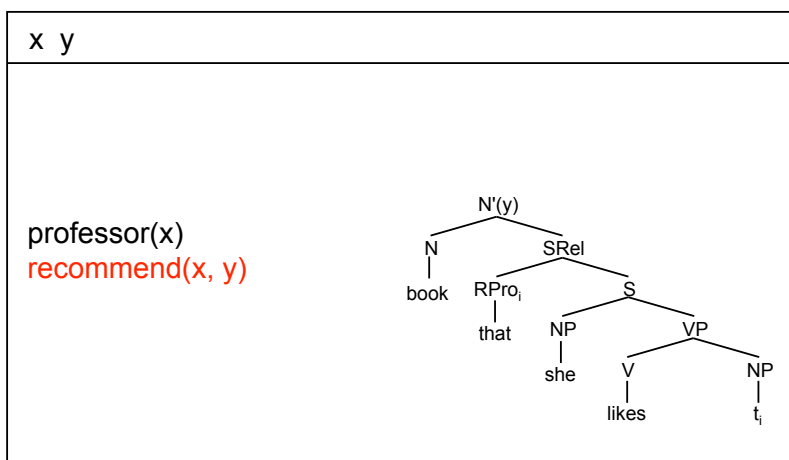
Indefinite NP rule



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Flattening



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DRS-CR for Relative Clauses

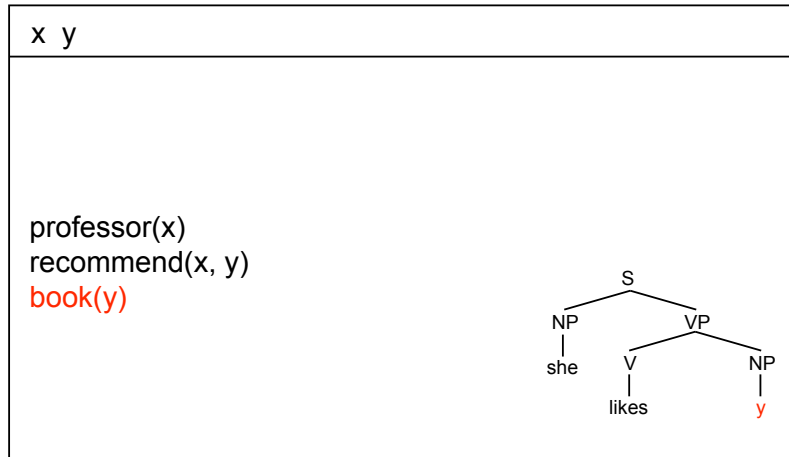


- Triggering configuration:
 - $\alpha(x)$ is reducible condition in DRS K ; α contains $[_{N'} [_{N'} \beta] [_{SRel} \gamma]]$ as a substructure
 - γ is relative clause of the form $\delta \epsilon$, where δ is a relative pronoun and ϵ a sentence with an NP gap t , δ and t are co-indexed.
- Actions:
 - Remove $\alpha(x)$ from C_K .
 - Add $\beta(x)$ to C_K .
 - Replace the NP gap in ϵ by x , and add the resulting structure to C_K .

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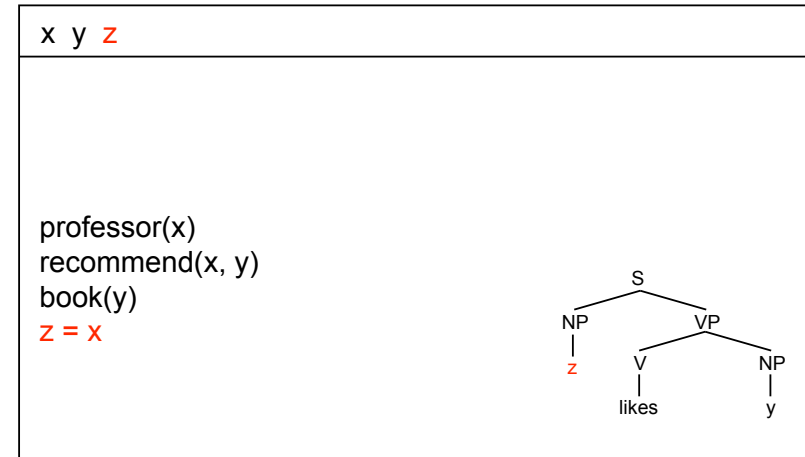
Relative Clause Rule



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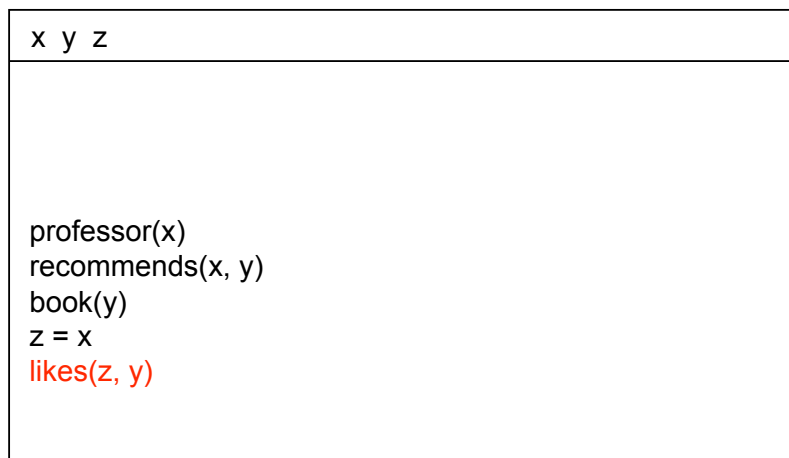
Personal Pronoun Rule



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Fully reduced DRS after Flattening



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A constraint on the DRS construction algorithm



- A problem: The basic DRS construction algorithm can derive DRSes for both of the following sentences, with the indicated anaphoric binding
 - *[A professor]_i recommends a book that she_i likes*
 - **She_i recommends a book that [a professor]_i likes*

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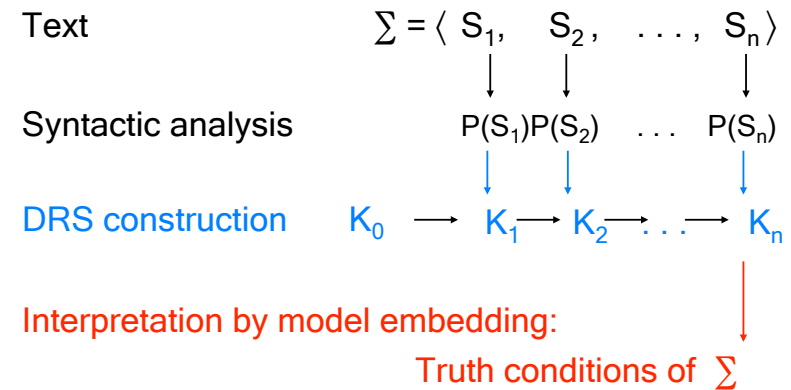
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The Highest Triggering Configuration Constraint



- If two triggering configurations of one or two different DRS construction rules occur in a reducible condition, then first apply the construction rule to the highest triggering configuration.
- The highest triggering configuration is the one whose top node dominates the top nodes of all other triggering configurations.

Discourse Representation Theory (DRT)



DRT: Denotational Interpretation



- Let
 - U_D a set of discourse referents,
 - $K = \langle U_K, C_K \rangle$ a DRS with $U_K \subseteq U_D$,
 - $M = \langle U_M, V_M \rangle$ a FOL model structure appropriate for K .
- An *embedding* of K into M is a (partial) function f from U_D to U_M such that $U_K \subseteq \text{Dom}(f)$.

Verifying embedding



- An embedding f of K in M verifies K in M :
 $f \models_M K$ iff f verifies every condition $\alpha \in C_K$.
- f verifies condition α in M ($f \models_M \alpha$):
 - (i) $f \models_M R(x_1, \dots, x_n)$ iff $\langle f(x_1), \dots, f(x_n) \rangle \in V_M(R)$
 - (ii) $f \models_M x = a$ iff $f(x) = V_M(a)$
 - (iii) $f \models_M x = y$ iff $f(x) = f(y)$

Example Computation



Let K be the example DRS from above:

$K = \langle \{x, y, z, u\}, \{ \text{professor}(x), \text{book}(y), \text{own}(x,y), \text{read}(z,u), z=x, u=y \} \rangle$

$f \models_M K$ iff f verifies every condition $\alpha \in C_K$, i.e.:

$f \models_M \text{professor}(x) \wedge f \models_M \text{book}(y) \wedge f \models_M \text{own}(x,y) \wedge f \models_M \text{read}(z,u) \wedge f \models_M z=x \wedge f \models_M u=y$

which holds iff:

$f(x) \in V_M(\text{professor}) \wedge f(y) \in V_M(\text{book}) \wedge \langle f(x), f(y) \rangle \in V_M(\text{own}) \wedge \langle f(z), f(u) \rangle \in V_M(\text{read}) \wedge f(z)=f(x) \wedge f(u)=f(y)$

Simplification



$f \models_M K$ iff

$f(x) \in V_M(\text{professor}) \wedge f(y) \in V_M(\text{book}) \wedge \langle f(x), f(y) \rangle \in V_M(\text{own}) \wedge \langle f(z), f(u) \rangle \in V_M(\text{read}) \wedge f(z) = f(x) \wedge f(u) = f(y)$

iff

$f(x) \in V_M(\text{professor}) \wedge f(y) \in V_M(\text{book}) \wedge \langle f(x), f(y) \rangle \in V_M(\text{own}) \wedge \langle f(x), f(u) \rangle \in V_M(\text{read}) \wedge f(u) = f(y)$

Simplification



$f \models_M K$ iff

$f(x) \in V_M(\text{professor}) \wedge f(y) \in V_M(\text{book}) \wedge \langle f(x), f(y) \rangle \in V_M(\text{own}) \wedge \langle f(z), f(u) \rangle \in V_M(\text{read}) \wedge f(z) = f(x) \wedge f(u) = f(y)$

iff

$f(x) \in V_M(\text{professor}) \wedge f(y) \in V_M(\text{book}) \wedge \langle f(x), f(y) \rangle \in V_M(\text{own}) \wedge \langle f(x), f(u) \rangle \in V_M(\text{read}) \wedge f(u) = f(y)$

iff

$f(x) \in V_M(\text{professor}) \wedge f(y) \in V_M(\text{book}) \wedge \langle f(x), f(y) \rangle \in V_M(\text{own}) \wedge \langle f(x), f(y) \rangle \in V_M(\text{read})$

Truth



- Let K be a closed DRS and M be an appropriate model structure for K .
- K is true in M iff there is a verifying embedding f of K in M such that $\text{Dom}(f) = U_K$

Basic features of DRT



- DRT models linguistic meaning as anaphoric potential (through DRS construction) plus truth conditions (through model embedding).
- In particular, DRT explains the ambivalent character of indefinite NPs: Expressions that introduce new reference objects into context, and are truth conditionally equivalent to existential quantifiers.

DRT: Extensions



- Conditionals, indefinites and anaphora
- Complex conditions
- Accessibility

Translation of DRSEs to FOL



- DRS $K = \langle \{x_1, \dots, x_n\}, \{c_1, \dots, c_k\} \rangle$

$x_1 \dots x_n$
$c_1 \dots c_n$

is truth-conditionally equivalent to the following FOL formula:

$$\exists x_1 \dots \exists x_n [c_1 \wedge \dots \wedge c_k]$$

Indefinite NPs and conditionals



Indefinite NPs and conditional clauses:

- *If a student works, the professor is happy.*
 - (1) $\exists x[\text{student}(x) \wedge \text{work}(x)] \rightarrow \text{happy_prof}$
 - (2) $\forall x[\text{student}(x) \wedge \text{work}(x) \rightarrow \text{happy_prof}]$
- Formulas (1) and (2) are logically equivalent:
 $\exists x A \rightarrow B \Leftrightarrow \forall x [A \rightarrow B]$
given that x doesn't occur free in B .

Indefinite NPs, Conditionals, and Anaphora



- *If a student works, he will be successful.*
 - (1) $\exists x[\text{student}(x) \wedge \text{work}(x)] \rightarrow \text{successful}(x)$
 - (2) $\exists x[\text{student}(x) \wedge \text{work}(x) \rightarrow \text{successful}(x)]$
 - (3) $\forall x [\text{student}(x) \wedge \text{work}(x) \rightarrow \text{successful}(x)]$

(1) is not closed
(2) has wrong truth conditions (much too weak)
(3) is correct, but how do you derive this compositionally?
- This is called the **donkey sentence problem**, with reference to the classical example by P.T. Geach (1967): *If a farmer owns a donkey, he beats it.*

Indefinite NPs and Discourse Structure



- *A car is parked in front of Peter's garage. Peter needs to get to the office quickly. He doesn't know who owns the car. He calls the police, and it is towed away.*
- *Suppose a car is parked in front of Peter's garage. Peter needs to get to the office quickly. He doesn't know who owns the car. Then he will call the police, and it will be towed away.*
- *Let a and b be two positive integers. Let b further be even. Then the product of a and b is even too.*

Context-dependent interpretation of indefinites

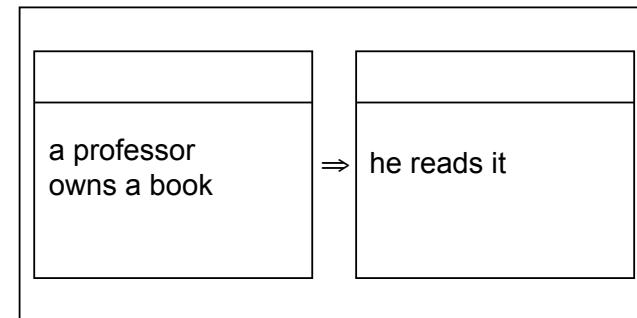


- The „quantificational force“ of indefinites depends on context:
 - Existential in plain assertions and narrative contexts
 - Universal in conditional or hypothetical reasoning.
- DRT offers uniform treatment in DRS construction, different truth conditional interpretation induced is by the respective context.

DRS for conditionals: An example



- *If a professor owns a book, he reads it.*



To be continued.