## FLST

# Grammars and Parsing 

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## What Happens in

## BETWEEN?



## What Happens in Between?


sound waves
activation of concepts

## What Happens in

## BETWEEN?


sound waves
Grammar
activation of concepts

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## THREE TRADITIONS



## Grammatik



$$
S \rightarrow N P V P
$$

## Grammatik



$$
S \rightarrow N P V P
$$

## Grammatik



$$
\begin{aligned}
& S \rightarrow N P \text { VP } \\
& \mathrm{VP} \rightarrow \mathrm{~V} \text { NP NP }
\end{aligned}
$$

## Grammar



$$
\begin{aligned}
& S \rightarrow N P \text { VP } \\
& \mathrm{VP} \rightarrow \mathrm{~V} \text { NP NP }
\end{aligned}
$$

$$
\vee \rightarrow \text { gave }
$$

single symbols strings
non-terminal
terminals
unspecified symbols
start symbol
empty string
integers

A, B, C, ...
$a, b, c, \ldots$
$\alpha, \beta, \gamma, \ldots$

S
e
$\ldots, \mathrm{i}, \mathrm{j}, \mathrm{k}, \mathrm{I}, \mathrm{m}, \mathrm{n}, \ldots$

## Why Syntax

- Einen Hund hat dieser Mann gebissen.
- Ein Hund hat diesen Mann gebissen.
- This man has bitten a dog.
- A dog this man has bitten.
- A dog has bitten this man.
- Peter promised Paul, to process the files.
- Peter persuaded Paul, to process the files.



## Formal Grammar

A language over an alphabet (vocabulary) $\Sigma$ is a subset of $\Sigma^{*}$.

A formal grammar $G_{L}$ for a language $L$ is a quadruple $\left(V_{N}, V_{T},\{S\}, P\right)$.
$\mathrm{V}_{\mathrm{N}}$ - non-terminal vocabulary (auxiliary vocabulary)
$\mathrm{V}_{\mathrm{T}}$ - terminal vocabulary

$$
\left(\mathrm{V}_{\mathrm{T}} \cap \mathrm{~V}_{\mathrm{N}}=\varnothing, \quad \mathrm{L} \subseteq \mathrm{~V}_{\mathrm{T}}^{*}, \quad \mathrm{~V}=\mathrm{V}_{\mathrm{T}} \cup \mathrm{~V}_{\mathrm{N}}\right)
$$

$\{S\}$ - singleton with the start symbol (set of axioms)

P - set of productions, rule set set of rules of the form $\omega_{1} \phi \omega_{2} \rightarrow \omega_{1} \psi \omega_{2}$ usually written as $\phi \rightarrow \psi$

## derivation

relation "follows":
If $G=\left(V_{N}, V_{T},\{S\}, P\right)$, then $\psi$ follows from $\phi$ according to $G$ iff there are strings $\phi_{1}$, $\phi_{2}, \chi, \omega$, so that $\phi=\phi_{1}, \chi, \phi_{2}$ und $\psi=\phi_{1}, \omega, \phi_{2}$ und
$\chi \rightarrow \omega \in P$.
Notation: $\quad \underset{\text { G }}{\#}$
derivation:
A sequence of strings $\phi_{1}, \phi_{1}, \ldots, \phi_{\mathrm{n}}$ is a derivation according to G iff $!_{\mathrm{i}} \quad!_{\mathrm{i}+1}$ for all $\mathrm{i}, 1 \leq \mathrm{i} \leq \mathrm{n}$.

If there is derivable according to G from $\phi$ to $\psi$ we can write this: ! $\quad \underset{\mathrm{G}}{\text { ( }}$
The relation derivable is transitive and is moreover defined to be reflexive.

The language $L$ : $A$ string $\omega$ is in $L$ according to $G_{L}$ iff the following three conditions are fulfilled:

1. $\omega \in V_{T}^{*}$
2. $\mathrm{S}_{\mathrm{G}}$ !
3. There is no $\chi$, so that ! \# and $\omega \neq \chi$.

G

We say that $G_{L}$ generates the language $L$. The language $L$ generated by $G$ is also written as $L(G)$.

Weak Equivalence: Two grammar $\mathrm{G}_{1}$ and $\mathrm{G}_{2}$ are weakly equivalent, if they generate the same language.

## Types of Grammars

## Type 0 (unrestricted rewriting systems):

Every formal grammar according to the definition is of type 0 .

## Type 1 (context sensitive grammars):

Every production is of the form $\phi \mathrm{A} \psi \rightarrow \phi \omega \psi$, where $A \in \mathrm{~V}_{\mathrm{N}}, \omega \neq \varepsilon$.

Type 2 (context free grammars):

Every production is of the form $\mathrm{A} \rightarrow \omega$, where $\omega \neq \varepsilon$.

Type 3 (regular grammars):
Every production is of the form $\mathrm{A} \rightarrow \mathrm{xB}$ or $\mathrm{A} \rightarrow \mathrm{x}$, where $\mathrm{x} \neq \varepsilon$.

# S <br> NP VP <br> DET ADJ N VP <br> DET ADJ N V NP DET ADJ N V DET ADJ N 

ein kleines Mädchen sucht ein kleines Mädchen

## Trees

## the notion of syntactic constituent tree

coded information

1. the hierarchic organisation of a sentence in terms of constituents
2. the assignment of each constituent to a linguistic class (category)
3. the linear sequence of the constituents

relations: immediate dominance - dominance
immediate precedence - precedence
constituent structure tree: quintuple( $\mathrm{N}, \mathrm{Q}, \mathrm{D}, \mathrm{P}, \mathrm{L}$ )
$N$ - finite set of nodes
Q - finite set of labels
D - weak partial order in $\mathrm{N} \times \mathrm{N}$, the dominance relation (reflexive, transitive und antisymmetric)
$P$ - strong partial order in $N \times N$, the precedence relation
(irreflexive, transitive und asymmetric)
L - function from N into Q , the labelling function

## conditions:

(single) root condition
exclusivity condition
no crossing condition / no tangling condition

## Conditions

## root condition

There is exactly one node that dominates all other nodes of the tree.

## exclusivity condition

For any two nodes $x$ and $y$ holds

$$
\begin{array}{ll}
\text { either } & D(x, y) \text { or } D(y, x) \\
\text { or } & P(x, y) \text { or } P(y, x) \\
\text { but never both. }
\end{array}
$$

no-tangling condition
If $P(x, y)$ then for all $x^{\prime}$ dominated by $x\left[D\left(x, x^{\prime}\right)\right]$ and for all $y^{\text {c }}$ dominated by $y\left[D\left(y, y^{\prime}\right)\right]$ that $x^{\prime}$ precedes $y^{\prime}\left[P\left(x^{\prime}, y^{\prime}\right)\right]$

## Parsing

- The syntactic analysis of strings according to a grammar we call parsing
- input: terminal string
output: structure of the sentence, i.e. all constituents usually a tree
- parsing algorithms:
top-down vs bottom-up
left-right vs right left vs birectional or island parsing
deterministic vs. non-deterministic


## Grammar

transformational grammar

## Grammar



