## Computational Linguistics Dependency-based Parsing

Clayton Greenberg
Stefan Thater

FR 4.7 Allgemeine Linguistik (Computerlinguistik)
Universität des Saarlandes
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## Phrase-Structure Trees



## Dependency Trees

- Basic idea:
- Syntactic structure = lexical items linked by relations
- Syntactic structures are usually trees (... but not always)
- Relations H $\rightarrow$ D
- H is the head (or governor)
- $D$ is the dependent



## Dependency Trees

- Parsers
- are easy to implement and evaluate
- Dependency-based representations
- are suitable for free word order languages
- are often close to the predicate argument structure



## Dependency Trees

- Some criteria for dependency relations between a head H and a dependent D in a linguistic construction C :
- H determines the syntactic category of $\mathrm{C} ; \mathrm{H}$ can replace C .
- H determines the semantic category of C; D specifies H .
- H is obligatory; D may be optional.
- H selects $D$ and determines whether $D$ is obligatory.
- The form of $D$ depends on $H$ (agreement or government).
- The linear position of $D$ is specified with reference to $H$.


## Dependency Trees

- Clear cases:
- Subject, Object, ...
- Less clear cases:
- complex verb groups
- subordinate clauses
- coordination


## Dependency Graphs

- Graph $G=\langle V, A, L,<\rangle$
- V = a set of vertices (nodes)
- A = a set of arcs (directed edges)
- L = a set of edge labels
- < = a linear order on V



## Dependency Trees - Notation



## Dependency Graphs / Trees

- Formal conditions on dependency graphs:
- $G$ is weakly connected
- G is acyclic
- Every node in G has at most one head
- G is projective


## Projectivity

- A dependency graph $G$ is projective iff
- if $w_{i} \rightarrow w_{j}$, then $w_{i} \rightarrow^{*} w_{k}$ for all $w_{i}<w_{k}<w_{j}$ or $w_{j}<w_{k}<w_{i}$
- if $w_{i}$ is the head of $w_{j}$, then there must be a directed path from $w_{i}$ to $w_{k}$, for all $w_{k}$ between $w_{i}$ and $w_{j}$.
- We need non-projectivity for
- long distance dependencies
- free word order



## Projectivity



## Projectivity

## Language Sentences Dependencies

| Arabic [Maamouri and Bies 2004] | $11.2 \%$ | $0.4 \%$ |
| ---: | :--- | :--- |
| Basque [Aduriz et al. 2003] | $26.2 \%$ | $2.9 \%$ |
| Czech [Hajic et al. 2001] | $23.2 \%$ | $1.9 \%$ |
| Danish [Kromann 2003] | $15.6 \%$ | $1.0 \%$ |
| Greek [Prokopidis et al. 2005] | $20.3 \%$ | $1.1 \%$ |
| Russian [Boguslavsky et al. 2000] | $10.6 \%$ | $0.9 \%$ |
| Slovenian [Dzeroski et al. 2006] | $22.2 \%$ | $1.9 \%$ |
| Turkish [Oflazer et al. 2003] | $11.6 \%$ | $1.5 \%$ |

## Dependency-based Parsing

- Grammar-based
- Data-driven
- Transition-based
- Graph-based


## Transition-based Parsing

- Configurations $\langle\mathrm{S}, \mathrm{Q}, \mathrm{A}\rangle$
- $\mathrm{S}=\mathrm{a}$ stack of partially processed tokens (nodes)
- $\mathrm{Q}=\mathrm{a}$ queue of unprocessed input tokens
- A = a set of dependency arcs
- Initial configuration for input $\mathrm{w}_{1} \ldots \mathrm{w}_{\mathrm{n}}$
- 〈[ $\left.\left.w_{0}\right],\left[w_{1}, \ldots, w_{n}\right],\{ \}\right\rangle, w_{0}=$ ROOT
- Terminal (accepting) configuration
- (..., [], ...)


## Transitions („Arc-Standard")

- Left-Arc(r)
- adds a dependency arc $\left(w_{j}, r, w_{i}\right)$ to the arc set $A$, where $w_{i}$ is the word on top of the stack and $w_{j}$ is the first word in the buffer, and pops the stack.
- Right-Arc(r)
- adds a dependency $\operatorname{arc}\left(w_{i}, r, w_{j}\right)$ to the $\operatorname{arc} \operatorname{set} A$, where $w_{i}$ is the word on top of the stack and $w_{j}$ is the first word in the buffer, pops the stack and replaces $w_{j}$ by $w_{i}$ at the head of buffer.


## Transitions („Arc-Standard")

- Left-Arc(r)

$$
\frac{\left\langle\left[\ldots, w_{i}\right],\left[w_{j}, \ldots\right], A\right\rangle}{\left\langle[\ldots],\left[w_{j}, \ldots\right], A \cup\left\{\left(w_{j}, r, w_{i}\right)\right\}\right\rangle} \quad i \neq 0, \neg \exists k \exists l^{\prime}\left(w_{k}, l^{\prime}, w_{i}\right) \in A
$$

- Right-Arc(r)

$$
\frac{\left\langle\left[\ldots, w_{i}\right],\left[w_{j}, \ldots\right], A\right\rangle}{\left\langle[\ldots],\left[w_{i}, \ldots\right], A \cup\left\{\left(w_{i}, r, w_{j}\right)\right\}\right\rangle} \quad \neg \exists k \exists l^{\prime}\left(w_{k}, l^{\prime}, w_{j}\right) \in A
$$

■ Shift

$$
\frac{\left\langle[\ldots],\left[w_{i}, \ldots\right], A\right\rangle}{\left\langle\left[\ldots, w_{i}\right],[\ldots], A\right\rangle}
$$

## An Example



Figure 2
Dependency graph for an English sentence from the Penn Treebank.

## An Example

|  | [0], | [1, ..., 9], | $\emptyset$ |
| :---: | :---: | :---: | :---: |
| SHIFT $\Longrightarrow$ | [0,1], | [2, ..., 9], | $\emptyset$ |
| LEFT-ARC ${ }_{\text {NMOD }} \Longrightarrow$ | [0], | [2, .., 9], | $A_{1}=\{(2, \mathrm{NMOD}, 1)\}$ |
| SHIFT $\Longrightarrow$ | [0,2], | [3, ..., 9], | $A_{1}$ |
| LEFT-ARC ${ }_{\text {SbJ }} \Longrightarrow$ | [0], | [3, ..., 9], | $A_{2}=A_{1} \cup\{(3, \mathrm{SBJ}, 2)\}$ |
| SHIFT $\Longrightarrow$ | [0,3], | [4, .., 9], | $A_{2}$ |
| SHIFT $\Longrightarrow$ | [0,3,4], | [ $5, \ldots, 9]$, | $A_{2}$ |
| LEFT-ARC ${ }_{\text {NMOD }} \Longrightarrow$ | [0,3], | [ $5, \ldots, 9]$, | $A_{3}=A_{2} \cup\{(5, \mathrm{NMOD}, 4)\}$ |
| SHIFT $\Longrightarrow$ | [0,3,5], | $[6, \ldots, 9]$, | $A_{3}$ |
| SHIFT $\Longrightarrow$ | [ $0, \ldots .6$ ], | [7, 8, 9], | $A_{3}$ |
| SHIFT $\Longrightarrow$ | [0, ..., 7], | [8,9], | $A_{3}$ |
| LEFT-ARC ${ }_{\text {NMOD }} \Longrightarrow$ | [0, .. 6], | [8,9], | $A_{4}=A_{3} \cup\{(8, \mathrm{NMOD}, 7)\}$ |
| RIGHT-ARC ${ }_{\text {PMOD }}^{\text {S }}$ ¢ | [0,3,5], | [6,9], | $A_{5}=A_{4} \cup\{(6$, PMOD, 8$)\}$ |
| RIGHT-ARC ${ }_{\text {NMOD }}^{\text {S }}$ ( | [0,3], | [ 5,9$]$, | $A_{6}=A_{5} \cup\{(5, \mathrm{NMOD}, 6)\}$ |
| RIGHT-ARC ${ }_{\text {OBJ }}^{s} \Longrightarrow$ | [0], | [3,9], | $A_{7}=A_{6} \cup\{(3$, OBJ, 5$)\}$ |
| SHIFT $\Longrightarrow$ | [0,3], | [9], | $A_{7}$ |
| RIGHT-ARC ${ }_{\text {P }}^{\text {S }}$ ¢ | [0], | [3], | $A_{8}=A_{7} \cup\{(3, \mathrm{P}, 9)\}$ |
| RIGHT-ARC ${ }_{\text {ROOT }}^{\text {S }}$ ¢ | [], | [0], | $A_{9}=A_{8} \cup\{(0$, ROOT, 3$)\}$ |
| SHIFT $\Longrightarrow$ | [0], | [], | $A_{9}$ |

## Deterministic Parsing

- oracle(c):
- predicts the next transition
- parse( $w_{1} \ldots w_{n}$ ):
- c:= $\left\langle\left[w_{0}=\right.\right.$ ROOT $\left.],\left[w_{1}, \ldots, w_{n}\right],\{ \}\right\rangle$
- while $c$ is not terminal
- $\mathrm{t}:=$ oracle(c)
- c:= t(c)
- return $G=\left\langle\left\{w_{0}, \ldots, w_{n}\right\}, A_{c}\right\rangle$


## Deterministic Parsing

- Linear time complexity: the algorithm terminates after 2 n steps for input sentences with n words.
- The algorithm is complete and correct for the class of projective dependency trees:
- For every projective dependency tree $T$ there is a sequence of transitions that generates $T$
- Every sequence of transition steps generates a projective dependency tree
- Whether the resulting dependency tree is correct or not depends of course on the oracle.


## The oracle

- Approximate the oracle by a classifier
- Represent configurations be feature vectors; for instance
- lexical properties (word form, lemma)
- category (part of speech)
- labels of partial dependency trees


## An Example

| f( $c_{0}$ ) | $=$ (root | Economic | news | NULL | null | nuLL | nulL) |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| f( $c_{1}$ ) | $=$ (Economic | news | had | null | null | null | nULL) |
| f( $c_{2}$ ) | $=$ (root | news | had | null | null | ATT | nULL) |
| f( $c_{3}$ ) | $=$ (news | had | little | ATT | NULL | NULL | nULL) |
| f( $c_{4}$ ) | $=$ (root | had | little | null | NULL | SBJ | nULL) |
| f(cs) | $=$ (had | little | effect | SBJ | null | null | nULL) |
| f( $c_{6}$ ) | $=$ (little | effect | on | null | nULL | null | null) |
| f( $c_{7}$ ) | $=$ (had | effect | on | SBJ | null | ATT | null) |
| f( $c_{8}$ ) | $=$ (effect | on | financial | ATT | null | null | null) |
| f(c9) | $=$ (on | financial | markets | null | null | null | null) |
| $\mathbf{f}\left(c_{10}\right)$ | $=$ (financial | markets | . | null | null | null | null) |
| f( $c_{11}$ ) | $=$ (on | markets | . | null | null | ATT | null) |
| f( $c_{12}$ ) | $=$ (effect | on |  | ATT | null | null | ATT) |
| f( $c_{13}$ ) | $=$ (had | effect | . | SBJ | NUL | ATT | ATT) |
| f( $c_{14}$ ) | $=$ (root | had |  | null | null | SBJ | OBJ) |
| f( $c_{15}$ ) | $=$ (had |  | null | SBJ | OBJ | null | null) |
| f( $c_{16}$ ) | $=$ (root | had | null | null | null | SBJ | PU) |
| f( $c_{17}$ ) | $=$ (nUlL | Rоot | null | null | NULL | null | PRED) |
| f( $c_{18}$ ) | $=$ (root | null | null | null | PRED | null | null) |

## Non-projective Parsing

- Configurations $\left\langle L_{1}, L_{2}, Q, A\right\rangle$
- $\mathrm{L}_{1}, \mathrm{~L}_{2}$ are stacks of partially processed nodes
- $\mathrm{Q}=\mathrm{a}$ queue of unprocessed input tokens
- A = a set of dependency arcs
- Initial configuration for input $w_{1} \ldots W_{n}$
- 〈[ $\left.\left.w_{0}\right],[],\left[w_{1}, \ldots, w_{n}\right],\{ \}\right\rangle, w_{0}=$ ROOT
- Terminal configuration:
- 〈[wo, $\left.w_{1}, \ldots, w_{n}\right],[],[], A$ )


## Transitions

- Left-Arc(I)

$$
\begin{array}{lr}
\left\langle\left[\ldots, w_{i}\right],[\ldots],\left[w_{j}, \ldots\right], A\right\rangle & i \neq 0 \\
\left\langle[\ldots],\left[w_{i}, \ldots\right],\left[w_{j}, \ldots\right], A \cup\left\{\left(w_{j}, l, w_{i}\right)\right\}\right\rangle & \neg \exists k \exists l^{\prime}\left(w_{k}, l^{\prime}, w_{i}\right) \in A \\
\neg w_{i} \rightarrow w_{j}^{*}
\end{array}
$$

- Right-Arc(I)

$$
\begin{array}{rr}
\left\langle\left[\ldots, w_{i}\right],[\ldots],\left[w_{j}, \ldots\right], A\right\rangle & \neg \exists k \exists I^{\prime}\left(w_{k}, l^{\prime}, w_{j}\right) \in A \\
\left\langle[\ldots],\left[w_{i}, \ldots\right],\left[w_{j}, \ldots\right], A \cup\left\{\left(w_{i}, l, w_{j}\right)\right\}\right\rangle & \neg w_{i} \rightarrow * w_{j}
\end{array}
$$

## Transitions

- No-Arc
$\frac{\left\langle\left[\ldots, w_{i}\right],[\ldots],[\ldots], A\right\rangle}{\left\langle[\ldots],\left[w_{i}, \ldots\right],[\ldots], A\right\rangle}$
- Shift

$$
\begin{aligned}
& \frac{\left\langle[\ldots]_{\mathrm{L} 1},[\ldots]_{\mathrm{L} 2},\left[\mathrm{w}_{\mathrm{i}}, \ldots\right], \mathrm{A}\right\rangle}{\left\langle[\ldots]_{\mathrm{L} 1} \cdot\left[\ldots, \mathrm{w}_{\mathrm{i}}\right]_{\mathrm{L} 2},[],[\ldots], \mathrm{A}\right\rangle} \\
& \mathrm{L}_{1} \cdot \mathrm{~L}_{2}=\text { the concatenation of } \mathrm{L}_{1} \text { and } \mathrm{L}_{2}
\end{aligned}
$$

## An Example

## AuxK



Figure 1
Dependency graph for a Czech sentence from the Prague Dependency Treebank.

## An Example

|  | $([0]$, | $[1$, | $[1, \ldots, 8], \emptyset$ |
| :---: | :--- | :--- | :--- |
| SHIFT $^{\lambda} \Longrightarrow([0,1]$, | [], | $[2, \ldots, 8], \emptyset$ |  |
| RIGHT-ARC |  |  |  |

## An Example

| No-ARC ${ }^{n} \Longrightarrow$ | [ $0, \ldots, 4$ ], [5], | [6,7,8], | $A_{5}$ |
| :---: | :---: | :---: | :---: |
| No-ARC ${ }^{n} \Longrightarrow$ | ( [0, .., 3], [4,5], | [6,7,8], | $A_{5}$ |
| Right-ARCAux ${ }_{\text {a }}^{n}$ ¢ | $[0,1,2], \quad[3,4,5]$, | $[6,7,8]$, | $A_{6}=A_{5} \cup\{(3, \operatorname{AuxP}, 6)\}$ |
| $\mathrm{SHIFT}^{\text {d }} \Longrightarrow$ | ( [0, .., 6], [], | [7,8], | $A_{6}$ |
| Right-ARC ${ }_{\text {Adv }}^{n} \Longrightarrow$ | [0, .., 5], [6], | [7,8], | $A_{7}=A_{6} \cup\{(6, \mathrm{Adv}, 7)\}$ |
| SHIFT ${ }^{\lambda}$ ¢ | ( [0, .., 7], [], | [8], | $A_{7}$ |
| NO-ARC ${ }^{n}$ ¢ | ( [0, .., 6], [7], | [8], | $A_{7}$ |
| No-ARC ${ }^{n} \Longrightarrow$ | ( [0, .., 5], [6,7], | [8], | $A_{7}$ |
| No-Arc ${ }^{n} \Longrightarrow$ | ( $[0, \ldots, 4],[5,6,7]$, | [8], | $A_{7}$ |
| No-ARC ${ }^{n} \Longrightarrow$ | ( [0, .., 3], [4, .., 7], | [8], | $A_{7}$ |
| No-ARC ${ }^{n} \Longrightarrow$ | ( [0, 1, 2], [3, ...7], | [8], | $A_{7}$ |
| No-ARC ${ }^{\text {n }}$ ¢ | ( [0, 1], [2, .., 7], | [8], | $A_{7}$ |
| No-ARC ${ }^{\text {n }}$ ¢ | ( [0], [1, . . 7 ], | [8], | $A_{7}$ |
| Right-Arc ${ }_{\text {AuxK }}^{n}=$ | ( [], [0, .., 7], | [8], | $A_{8}=A_{7} \cup\{(0, \mathrm{AuxK}, 8)\}$ |
| SHIFT ${ }^{\text { }}$ | ( [0, .. 8 ], [], | [], | $A_{8}$ |

## Non-projective Parsing

- The algorithm is sound and complete for the class of dependency forests
- Time complexity is $\mathrm{O}\left(\mathrm{n}^{2}\right)$
- at most n Shift-transitions
- between the i-th and (i+1)-th Shift-transition there are at most i transitions (left-arc, right-arc, no-arc)


## Literature

- Sandra Kübler, Ryan McDonald and Joakim Nivre (2009). Dependency Parsing.
- Joakim Nivre (2008). Algorithms for Deterministic Incremental Dependency Parsing. Computational Linguistics 34(4), 513-553.

